

DEDUCTIONS

PHIL 140A

SPRING 2016

1. Show that the following propositions are derivable:

(a) $\neg(\varphi \wedge \neg\psi) \rightarrow (\varphi \rightarrow \psi)$

(b) $((\varphi \rightarrow \psi) \wedge (\varphi \rightarrow \neg\psi)) \rightarrow \neg\varphi$

(c) $\neg(\varphi \rightarrow \psi) \rightarrow (\psi \rightarrow \varphi)$

(d) $\neg(\varphi \rightarrow \psi) \rightarrow (\varphi \rightarrow \neg\psi)$

2. Show that the following rules are derivable in our deduction system:

$$\frac{\neg\neg\varphi}{\varphi} \neg\neg E$$

$$\frac{\varphi \rightarrow \psi}{\neg\psi \rightarrow \neg\varphi} \text{CP}$$

3. Suppose we replaced RAA with $\neg\neg E$ for only atomic formulas. Show that the full $\neg\neg E$ would still be derivable.