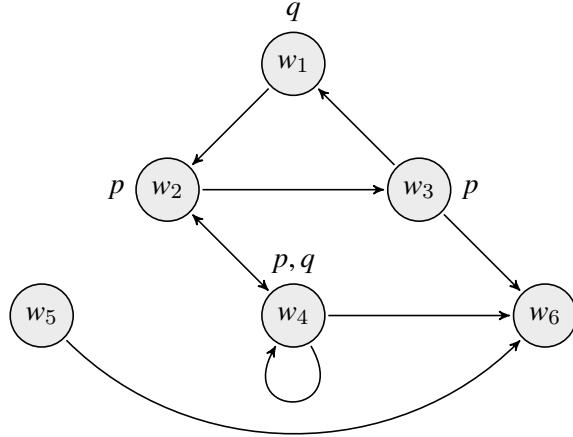


Modal Truth & Bisimulations

Phil 143 Worksheet

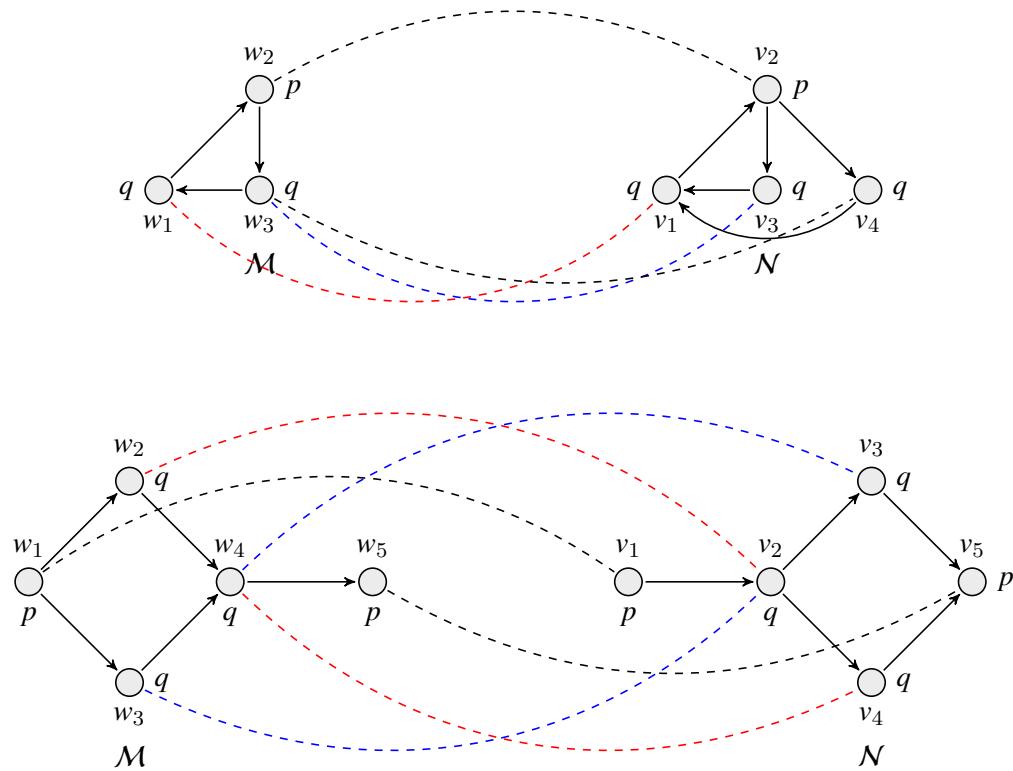
1. Consider the following diagram:



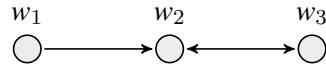
Which states are the following formulas true?

- | | |
|---|---|
| (a) $\Diamond(p \wedge q)$ | (j) $\Diamond p$ |
| w_2, w_4 | w_1, w_2, w_4 |
| (b) $\Diamond(p \wedge \neg q)$ | (k) $\Diamond\Diamond p$ |
| w_1, w_2, w_4 | w_1, w_2, w_3, w_4 |
| (c) $\Diamond\Diamond(p \wedge q)$ | (l) $\Box\Diamond p$ |
| w_1, w_2, w_4 | w_1, w_6 |
| (d) $\Box\Diamond(p \wedge \neg q)$ | (m) $\Diamond\Box p$ |
| w_1, w_6 | w_1, w_3, w_4, w_5 |
| (e) $\Box\perp$ | (n) $\Box\Box p \rightarrow \Box p$ |
| w_6 | w_1, w_2, w_4, w_6 |
| (f) $\Diamond\Box\perp$ | (o) $\Diamond\Diamond p \rightarrow \Diamond p$ |
| w_3, w_4, w_5 | w_1, w_3, w_4, w_5, w_6 |
| (g) $\Diamond\Diamond\Diamond\Box\perp$ | (p) $\Box\Diamond p \rightarrow \Diamond p$ |
| w_1, w_2, w_4 | w_1, w_2, w_3, w_4, w_5 |
| (h) $\Box p$ | (q) $\Diamond\Box p \rightarrow \Box p$ |
| w_1, w_2, w_6 | w_1, w_2, w_6 |
| (i) $\Box\Box p$ | (r) $\Box\Diamond p \rightarrow \Diamond\Box p$ |
| w_1, w_3, w_5, w_6 | w_1, w_2, w_3, w_4, w_5 |

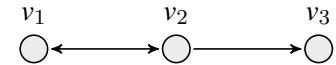
2. Draw a bisimulation between the models \mathcal{M} and \mathcal{N} connecting w_1 and v_1 :



3. Find a formula that w_1 and v_1 disagree on in the models below:



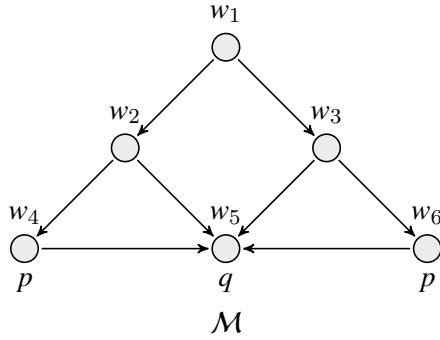
\mathcal{M}



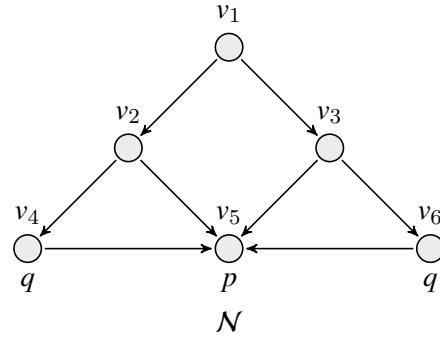
\mathcal{N}

Above: $\mathcal{N}, v_1 \models \diamond\diamond\Box\perp$ but $\mathcal{M}, w_1 \not\models \diamond\diamond\Box\perp$.

Below: $\mathcal{M}, w_1 \models \diamond\diamond\diamond q$, but $\mathcal{N}, v_1 \not\models \diamond\diamond\diamond q$ (reversed for $\diamond\diamond\diamond p$).



\mathcal{M}



\mathcal{N}